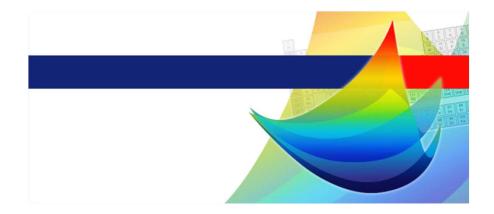


DICTRA On-line Training

14 – 16 October 2025



www.thermocalc.com

Schedule



Diffusion Module (DICTRA)

Day	1
-----	---

9:00	Introduction to DICTRA (= Diffusion Module)
9:40	Example - Up-hill diffusion in the Fe-Si-C system
10:25	Q&A
10:40	Example – Carburisation and de-carburisation
11:10	Example – Particle growth
11:45	Q&A
12:00	Home assignment 1

Schedule



Diffusion Module (DICTRA)

Day	2
-----	---

9:00	Home assignment 1
9:10	Example - Solidification using Scheil
9:30	Example - Scheil with real back-diffusion in the solid.
9:50	Example – DICTRA solidification (Moving phase boundary)
10:30	Q&A
10:45	Diffusion theory and numerics
11:15	Example – Homogenisation model: Diffusion couple
11:45	Q&A
12:00	Home assignment 2

Schedule



Diffusion Module (DICTRA)

Day 3	3
-------	---

9:00	Home assignment 2
9:10	Example – Dissolution of cementite particles
	(moving phase boundary calculation)
10:10	Console mode and macro files.
10:30	Q&A
10:45	Example – Gradient sintering in Cemented carbide
11:30	Trouble shooting
11:45	Q&A
12:00	End

Course material



The download link for the course material is: https://download.thermocalc.com/training/Diff-Day1/

This folder **Diff-Day1** contains the files:

DICT-Day1.pdf pdf of all today's slides.

The-Role-of-Diffusion-in-Materials-Tutorial_Thermo-Calc-Software.pdf (note Chapter 2 on Diffustion theory).

Folders for Day2 and Day3 are already, or will be, available at

https://download.thermocalc.com/training/Diff-Day2 https://download.thermocalc.com/training/Diff-Day3

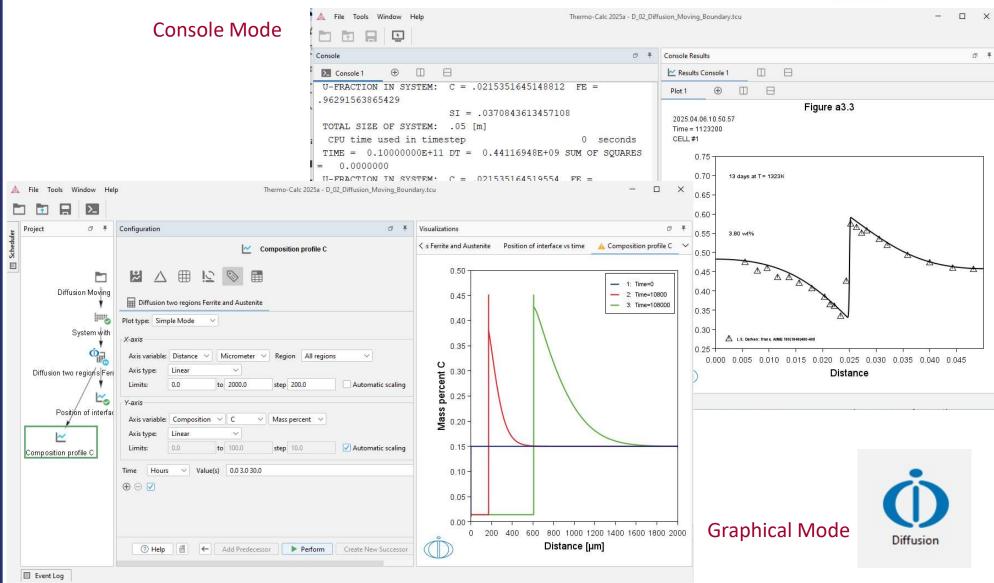
The Software



- ☐ Software package for simulation of diffusion controlled reactions in multi-component alloys.
- ☐ Simulation on geometries, which may be reduced to one spatial coordinate (planar, cylindrical or spherical)
- ☐ Linked to Thermo-Calc, which provides all necessary thermodynamic properties.
- ☐ Development started 40 years ago at:
 - Royal Institute of Technology in Stockholm, Sweden
 - MPI für Eisenforschung in Düsseldorf, Germany (only very early)
 - Thermo-Calc Software AB (from 1997 and on)

Overview of Diffusion Module 2025b

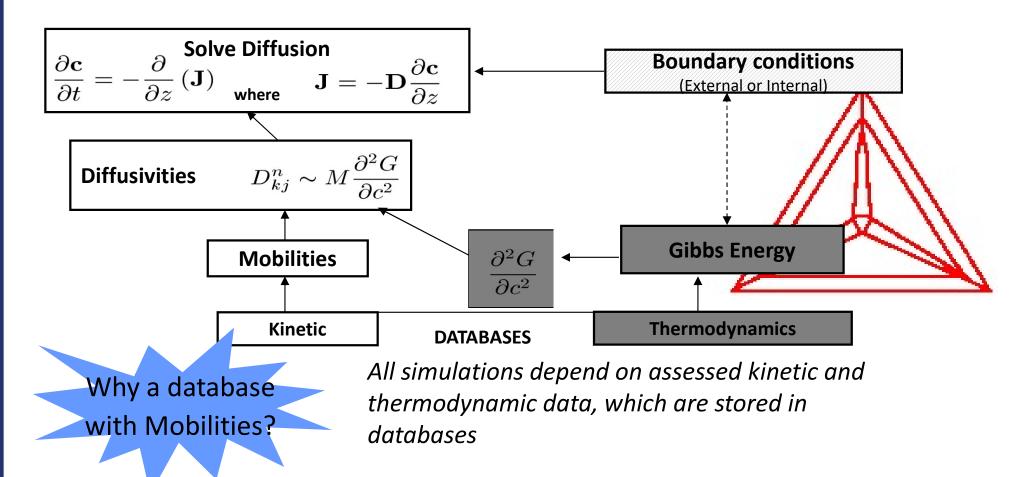




Basic calculation procedure

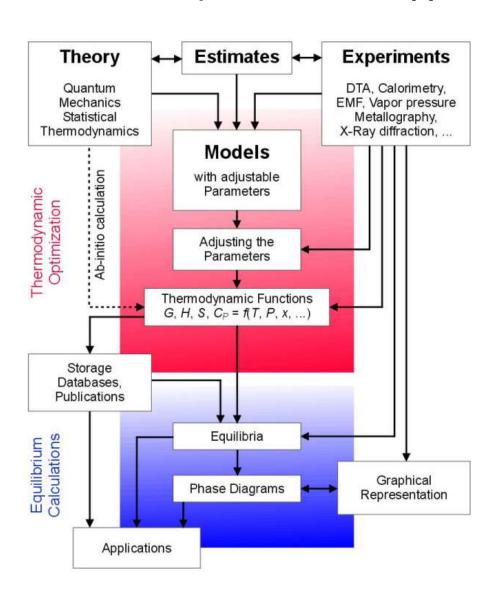


A numerical finite difference scheme is used for solving a system of coupled parabolic partial differential equations



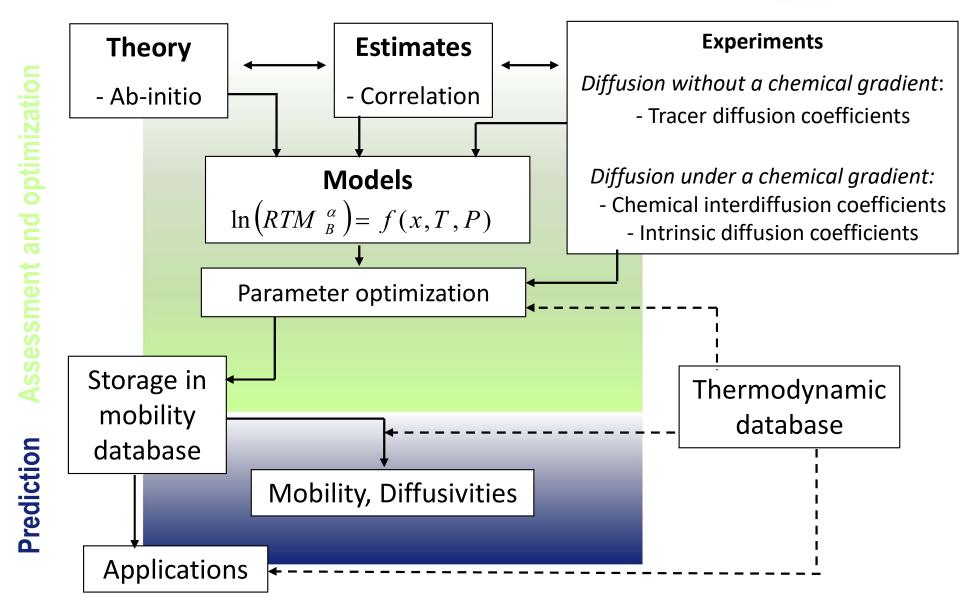
Thermodynamic Databases (The CALPHAD approach)





Kinetic Databases (in a CALPHAD spirit)





Modelling of the atomic mobility



From absolute reaction-rate theory arguments Andersson and Ågren¹⁾ suggested:

When treating the composition dependency of the mobility, Jönsson²⁾ found it superior to expand the logarithm of the mobility rather than the value itself, i.e.

$$RT \ln [RTM_B] = RT \ln M_B^0 - Q_B$$

Because $\ln[RTM_i]$ is often found to have a fairly linear composition dependency

1. Andersson, Ågren, J Appl Phys 72(1992)1350

2. Jönsson, Scand J Metall 24(1995)21

Composition dependency



In a CALPHAD spirit the composition dependency is represented with a linear combination of the values at each endpoint of the composition space, and a Redlich-Kister expansion, i.e.

$$\Phi_B = \sum_{i} x_i \Phi_B^i + \sum_{i} \sum_{j>i} x_i x_j \left[\sum_{r=0}^{m} {}^r \Phi_B^{i,j} (x_i - x_j)^r \right]$$

where Φ_B represents $RT \ln M_B^0 - Q_B$

Example: FCC Ni-Al

Ni A

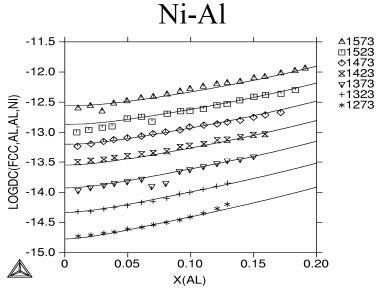
 $\Phi_{Ni}^{\ Ni}$

 \mathbf{P}_{Ni}^{Al}

 $\Phi_{Ni}^{~Al~,Ni}$

 Φ_{Al}^{Al}

 $\Phi_{Al}^{Al,Nl}$

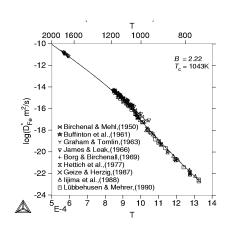


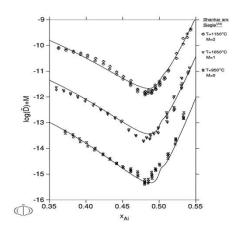
Engström, Ågren, Z Metallkd 87(1996)92

Other effects on mobility



- ✓ Ferromagnetic ordering
- ✓ Chemical ordering
 can have very strong effects on the mobility and are described by a
 separate term each in the mobility expression.





Mobility enhancement in grain boundaries or dislocations are not taken into account in the mobility databases. It can be handled in the software by entering cross sectional area fractions and a factor reducing the activation energy compared to the bulk (console mode only).

DICTRA application types



- ☐ Diffusion in single-phase systems
- ☐ Diffusion with moving interfaces
- Cell calculations (particle distributions, immobile interfaces etc.) only in Console mode or <u>use TC-PRISMA</u>
- Diffusion in dispersed systems only in Console mode, use
- Homogenization model
- Coarsening or Ostwald ripening <u>- use TC-PRISMA</u>
- Growth of pearlite Console mode only, very little used.

DICTRA application types

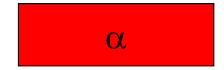


Diffusion in single-phase systems Diffusion with moving interfaces Cell calculations (particle distributions, immobile interfaces etc.) - only in Console mode or use TC-PRISMA Diffusion in dispersed systems – only in Console mode, use Homogenization model Coarsening or Ostwald ripening - use TC-PRISMA Growth of pearlite - Console mode, very little used

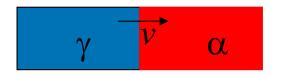
DICTRA application types



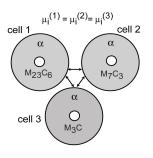
Single phase



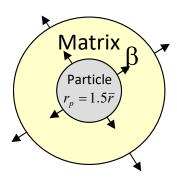
Moving boundary



Cell



Coarsening



Disperse system



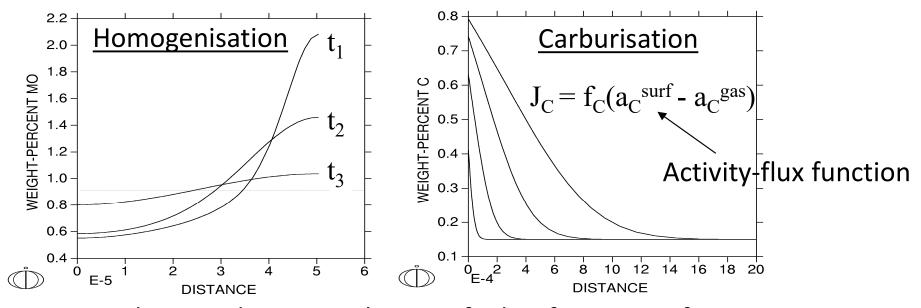
Homogenization



Diffusion in single-phase systems



Straight-forward non-complex simulations, usually on homogenisation or carburisation treatments



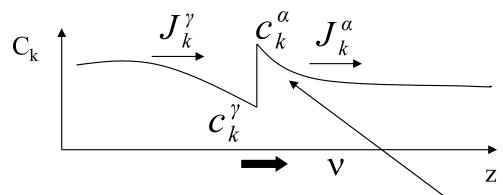
Boundary conditions can be specified as functions of time, temperature and pressure.

Different functions may be used in different time intervals.

Also: Spatially non-isothermal simulations

Diffusion with a moving interface





n-1 unknowns:

n-2 chemical potentials. Velocity of phase boundary, ν

n-1 Flux Balance Equations:

$$v\left(c_k^{\alpha} - c_k^{\gamma}\right) = J_k^{\alpha} - J_k^{\gamma}$$

Sharp interface with assumption of local equilibrium (also para-equilibrium possible)

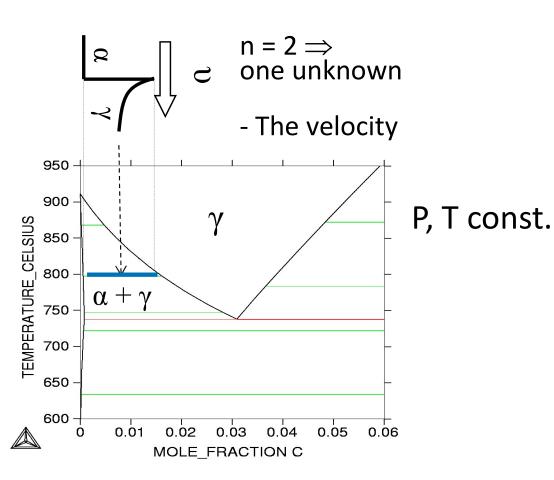
F-B Equations solved as:

$$\sum_{k=1}^{n-1} \left[v \left(c_k^{\alpha} - c_k^{\gamma} \right) - \left(J_k^{\alpha} - J_k^{\gamma} \right) \right]^2 < \varepsilon$$

Diffusion with a moving interface



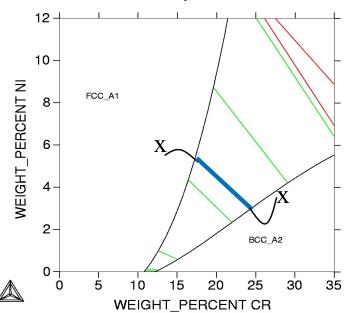
Binary example: Fe-C



Ternary example: Fe-Cr-Ni

 $n = 3 \Rightarrow two unknowns!$

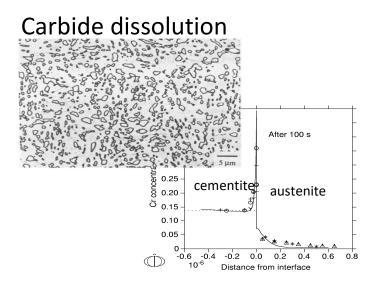
- One a_i or μ_i (i.e. one tie-line)
- The velocity



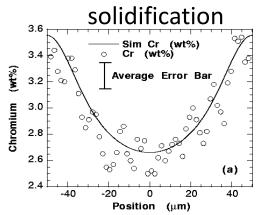
Some application examples



- \Box γ to α transformations in steel
- ☐ Growth and dissolution of particles
- Microsegregation during solidification
- \Box σ -phase precipitation in stainless steels
- ☐ Transient Liquid-Phase bonding of alloys
- Sintering of cemented carbides
- lacksquare and much more ...

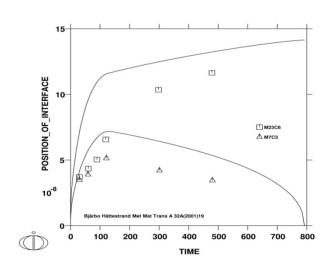


Microsegregation during

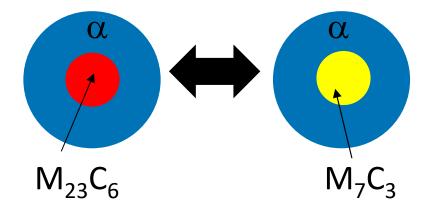


Cell calculations





- Growth or dissolution of particle distributions
- Competing growth or dissolution
- Interdiffusion across an immobile interface



Conditions for cell boundaries:

 \checkmark Equal diffusion potentials $\Phi_{\rm i}$ for the elements

$$\Phi_i = \mu_i - \mu_n$$
 for subst. elements $\Phi_i = \mu_i$ for interstitial elements

✓ Flux balances to conserve the mass of the elements

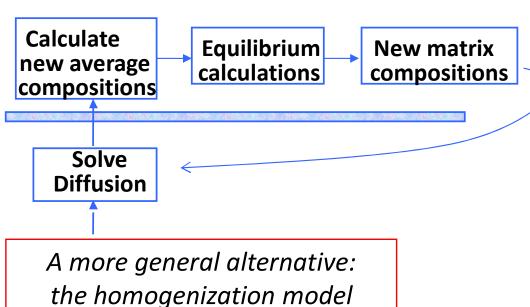
$$rac{J_i^{ ext{cell}\#1}}{n^{ ext{cell}\#1}} = rac{J_i^{ ext{cell}\#2}}{n^{ ext{cell}\#2}}$$
 n, cell distribution factors

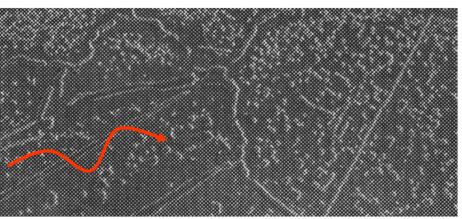
Diffusion in dispersed systems



Assumptions:

- Diffusion takes place in the matrix phase only.
- Equilibrium holds locally in each node.





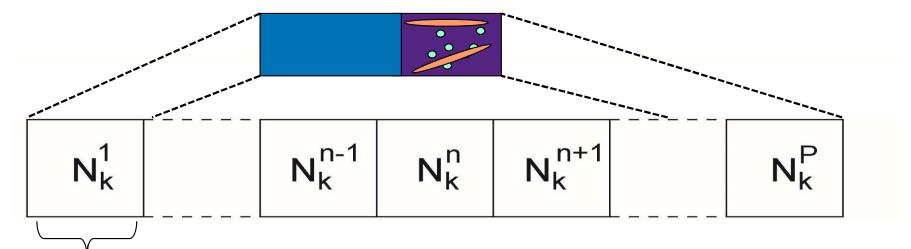
- Carburisation of high-temperature alloys
- Interdiffusion in composite materials
 - coating/substrate systems
 - weldments between steels
 - > joints of dissimilar steels
- Gradient sintering of cemented carbide work-tool pices

Engström et al, Met Mat Trans A 25A(1994)1127

Homogenization model



This approach allow us to account for diffusion in more than one phase



Equilibrium calculation for each slice

Phase fractions
Phase compositions
Chemical potentials
Mobilities

Flux between slices "n-1" and "n"

$$J_k = \frac{-1}{V_m} \sqrt{\left[M_k x_k\right]_{n-1}^{eff} \left[M_k x_k\right]_n^{eff}} \frac{\Delta \mu_k}{\Delta z}$$

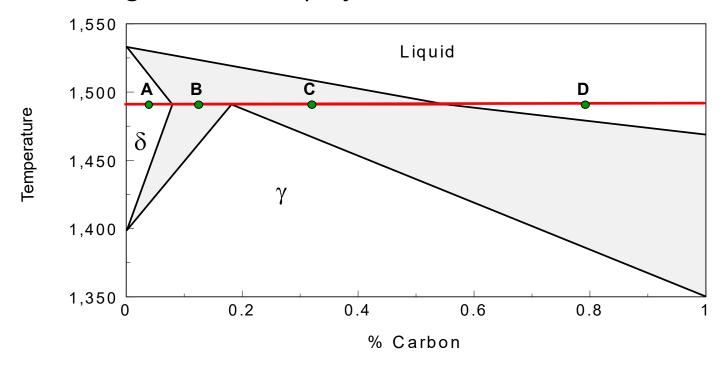
"Effective" $[M_k x_k]$ from combining rules

Larsson, Engström, Acta Mater 54(2006)2431 Larsson, Höglund, Calphad 33(2009)495

Case study: Micro-segregation during solidification



- ☐ VESPISM (Virtual Experiments to Solve Problems In Steel Metallurgy).
- ☐ Development of phase-field code (MICRESS) linked to Thermo-Calc.
- □ Solidification experiments were performed for alloys A − D below as one assignment in this project.

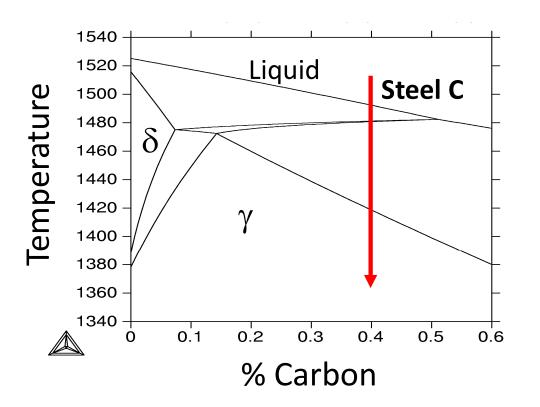


Observed micro-segregation in Steel C

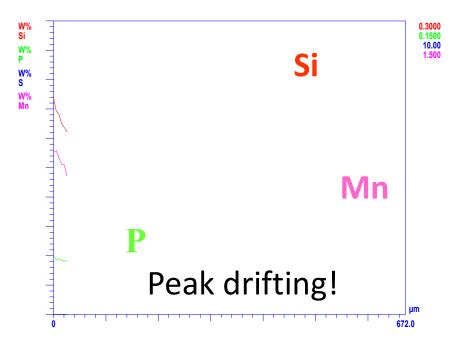


Steel C:

Fe -
$$0.8\%$$
 Mn $- 0.7\%$ Si $- 0.03\%$ P $- 0.4\%$ C



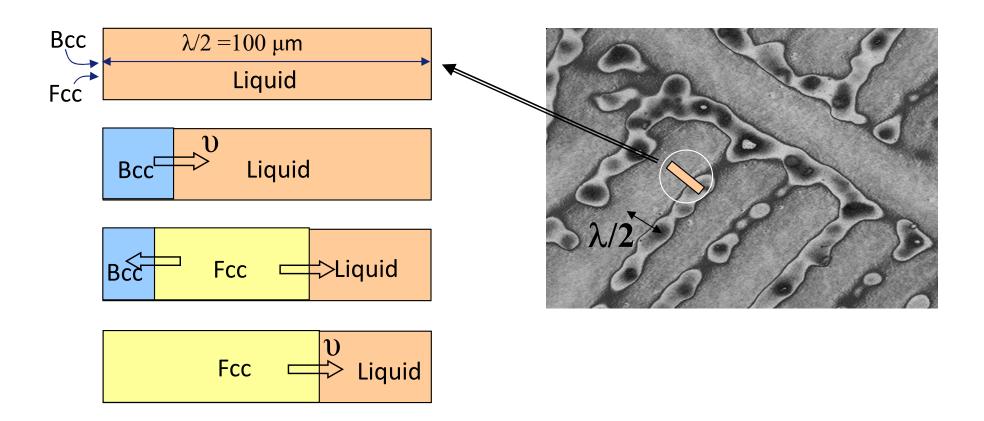
Line-scans across the dendrite arms (performed by Corus-UK)



Question: Why does the P peak drift away from the Mn and Si peaks?

Analysis using DICTRA

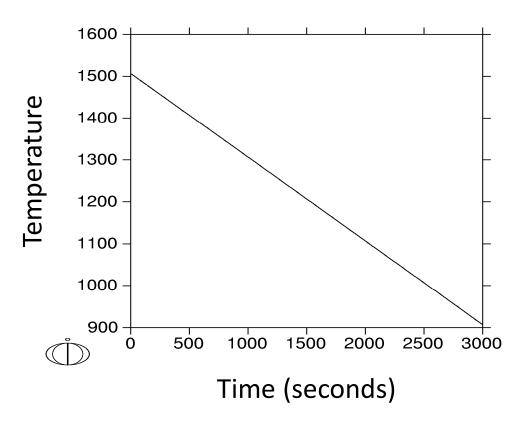




• Secondary dendrite arm spacing assumed to be 200 μ m.

Cooling function



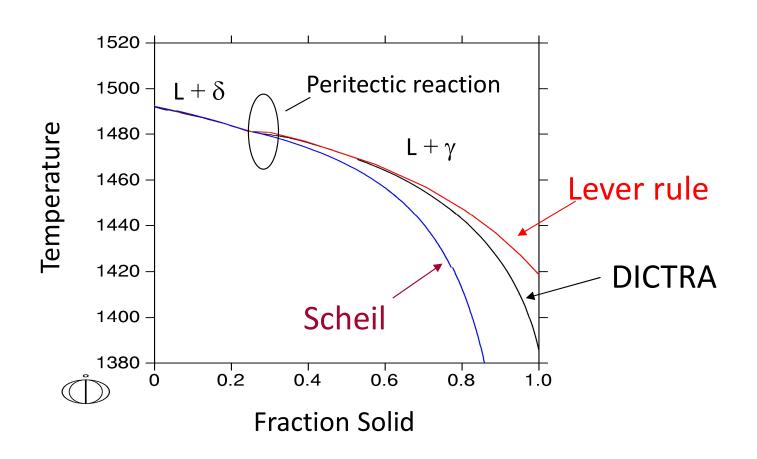


Cooling rate assumed to be 0.2 °C/s

- More advanced cooling functions may of course also be imposed.
- Also possible to instead define a condition on the rate of latent heat removal from the system.

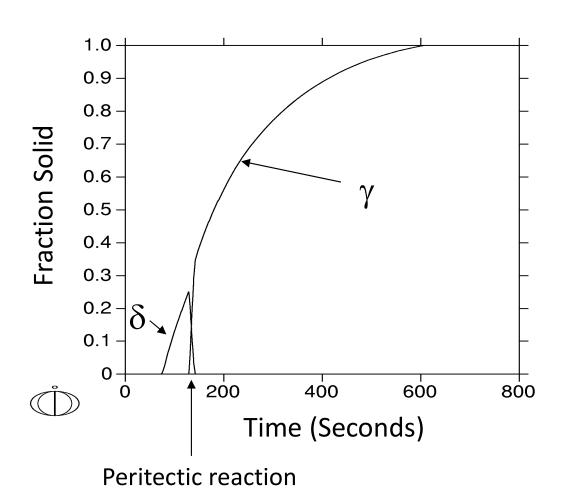
Solidification range





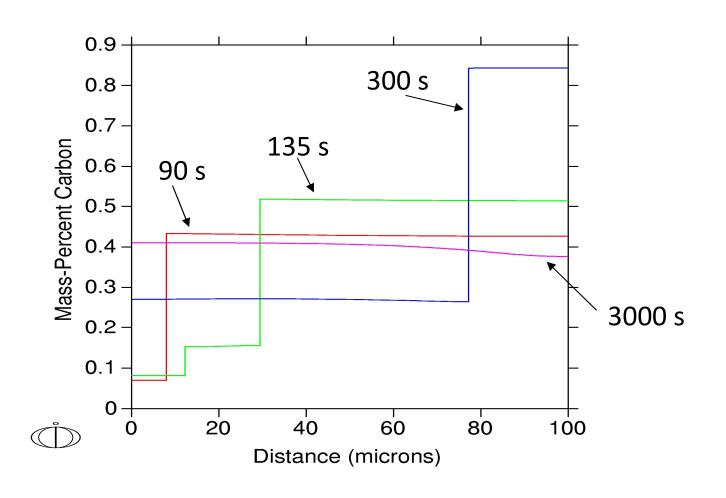
Fraction of solid phases





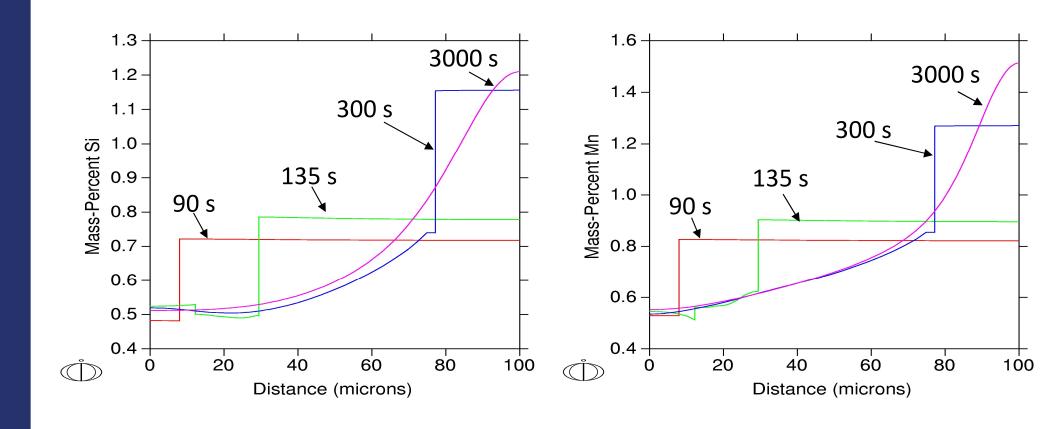
Carbon profiles during solidification





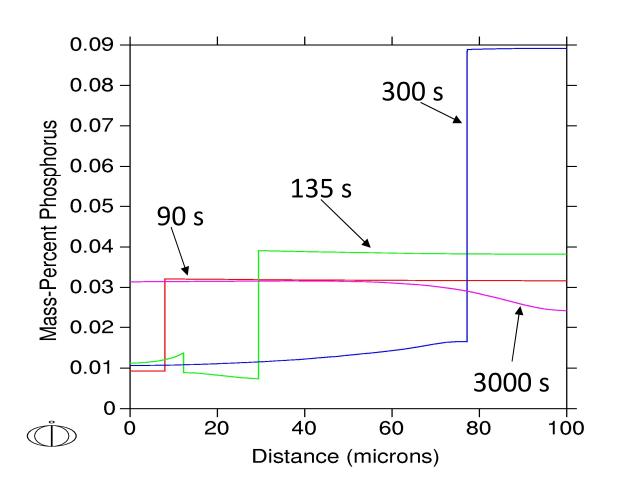
Silicon and Manganese





Phosphorus

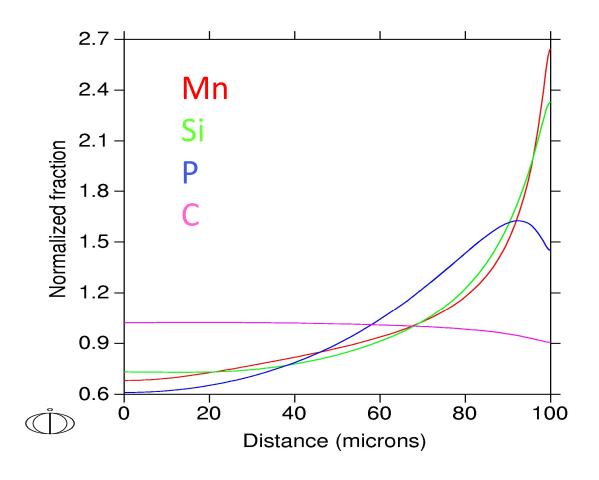




Segregation profiles after 610 s

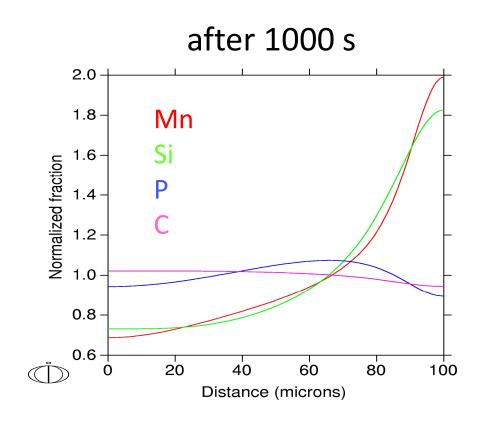


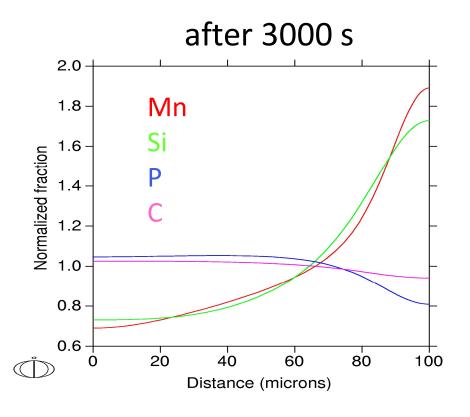
(when the last liquid disappears)



Segregation profiles after 1000 and 3000 s

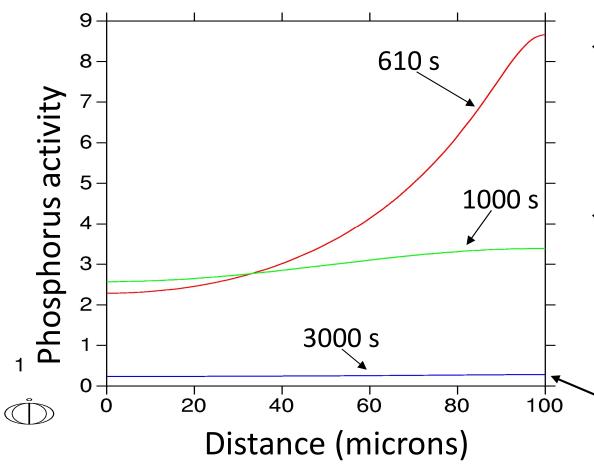






The solution





✓ Mn and Si increase the phosphorus activity.

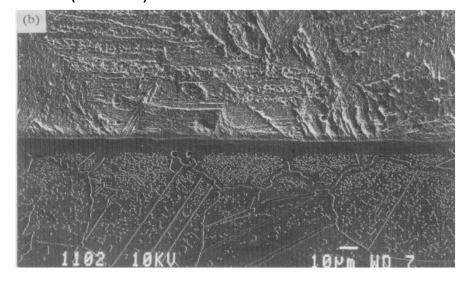
✓ Phosphorus diffusion much faster compared to Mn and Si diffusion.

At the late stage further phosphorus redistribution is controlled by slow Mn and Si diffusion.

Compound tubes for waste incinerators

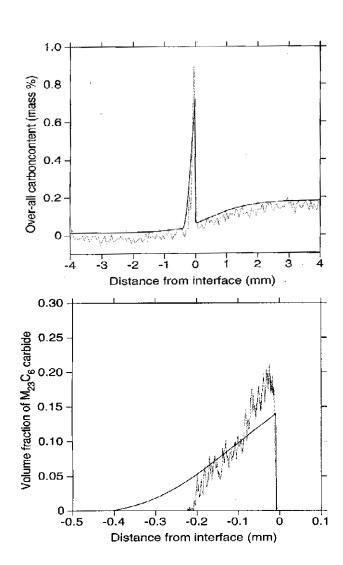


4L7 (0.18% C) After 4 h at 1100 °C



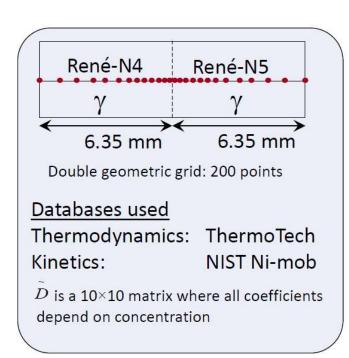
Sanicro28 (30.5% Ni, 27% Cr, 3.3% Mo, 1.8% Mn, 0.014% C)

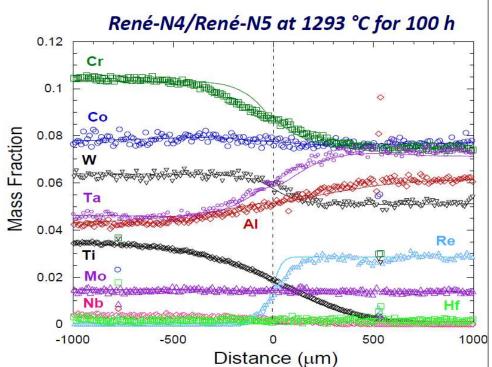
Helander, Ågren, Nilsson, ISIJ Int 37(1997)1139



Interdiffusion in Ni-superalloys







From: C. E. Campbell, Metallurgy Division, NIST

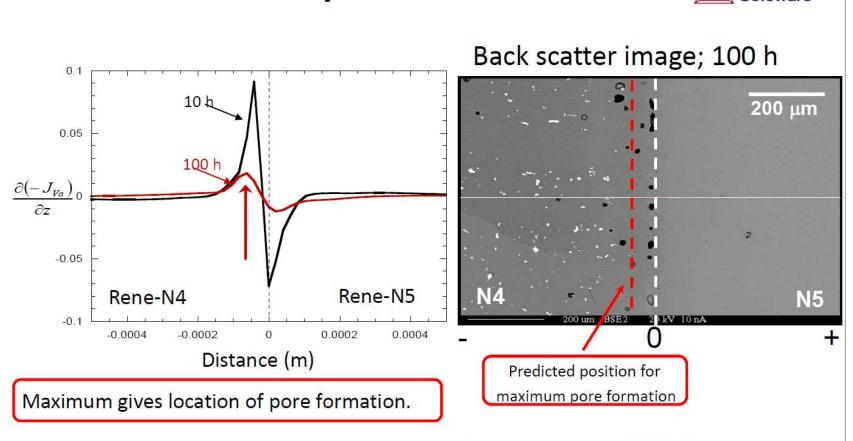
See also: Campbell et al, Mat Sci Eng A 407(2005)135

Experimental work performed by T. Hansen, P. Merewether, B. Mueller, Howmet Corporation, Whitehall, MI.

Interdiffusion in Ni-superalloys



Kirkendall porosity prediction



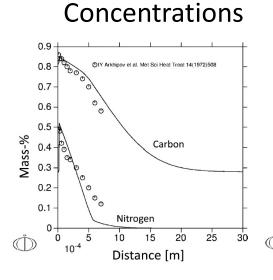
From: C. E. Campbell, Metallurgy Division, NIST

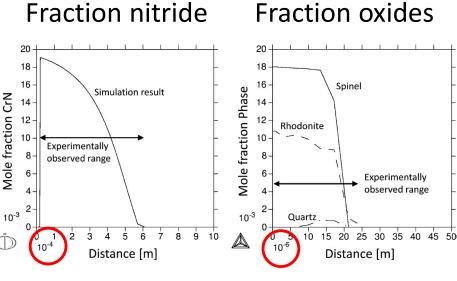
See also: Campbell et al, Mat Sci Eng A 407(2005)135

Coupled carbonitriding and internal oxidation



Fe-0.28C-1.15Cr-0.95Mn-0.27Si 850°C, 24 h





Micrograph and experimental data Arkhipov et al Met Sci Heat Treat 14(1972)508

Larsson, Ågren, HTM J Heat Treatm Mat 72(2017)19

Compatibility of Databases



Thermodynamic Database	Kinetic Database
SSOL2, SSOL4, SSOL5, SSOL6, SSOL7, SSOL8, SSOL9	MOB2
TCFE5 and earlier versions	MOB2
TCHEA2, TCHEA3+4+5, TCHEA6+7+8	MOBHEA1, MOBHEA2, MOBHEA3
TCFE6, 7, 8, 9, TCFE10, TCFE11, TCFE12, TCFE13+14	MOBFE1, 2, 3, 4, 5, 6, 7, MOBFE8
TTNI8 and earlier versions	MOBNI1
TCNI4, TCNI5, TCNI6*	MOBNI2*
TCNI7, TCNI8	MOBNI3, MOBNI4
TCNI9+TCNI10+TCNI11, TCNI12+TCNI13	MOBNI5, MOBNI6
TTAL8 and earlier versions	MOBAL1
TCTI4, TCTI5, TCTI6	MOBTI4
TCAL1+2+3, TCAL4,TCAL5, TCAL6+7, TCAL8, TCAL9	MOBAL3,4,5, MOBAL6, MOBAL7, MOBAL8
TCMG1+2+3+TCMG4+TCMG5, TCMG6	MOBMG1, MOBMG2
TCCU1, TCCU2, TCCU3, TCCU4, TCCU5 + TCCU6	MOBCU1, 2, 3, 4, MOBCU5

^{*} Pairing of TCNI6 and MOBNI2 is not possible for the LIQUID phase.



Some DICTRA specific concepts.

Terminology needed mostly for Console Mode

Region



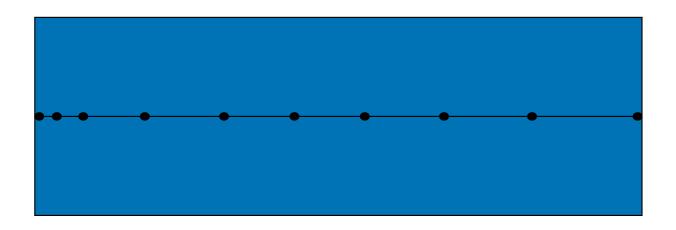


A "box" filled with the phase(s) where diffusion takes place. Can be given any name.

The region has two boundaries, left and right.

Grid

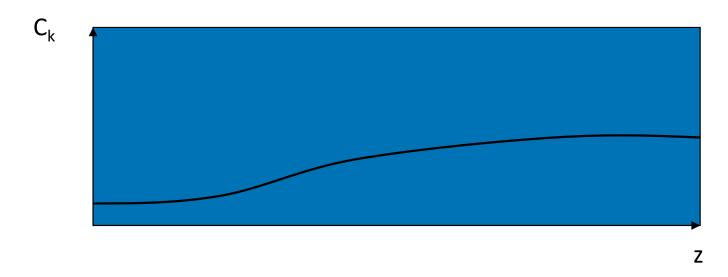




Distribution of node points for numerical calculations (inside the region).

Concentration Profile

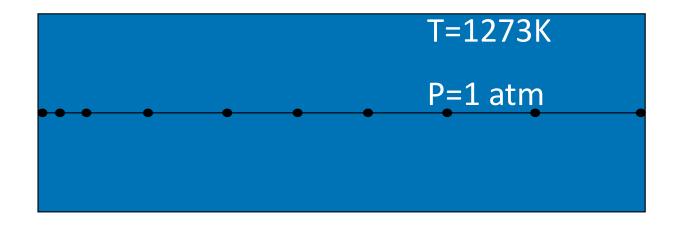




Concentration, C_k of an element as a function of distance z.

Global Conditions

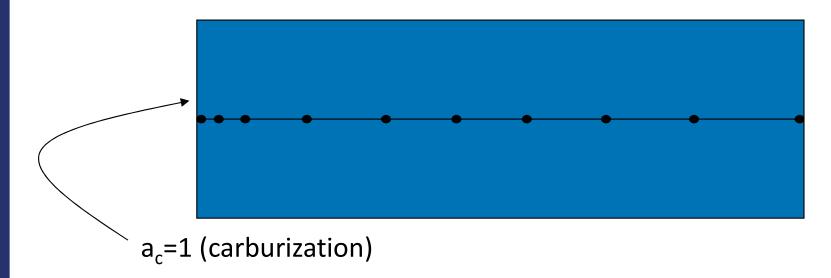




Conditions valid for entire system, T and P.

Boundary Conditions

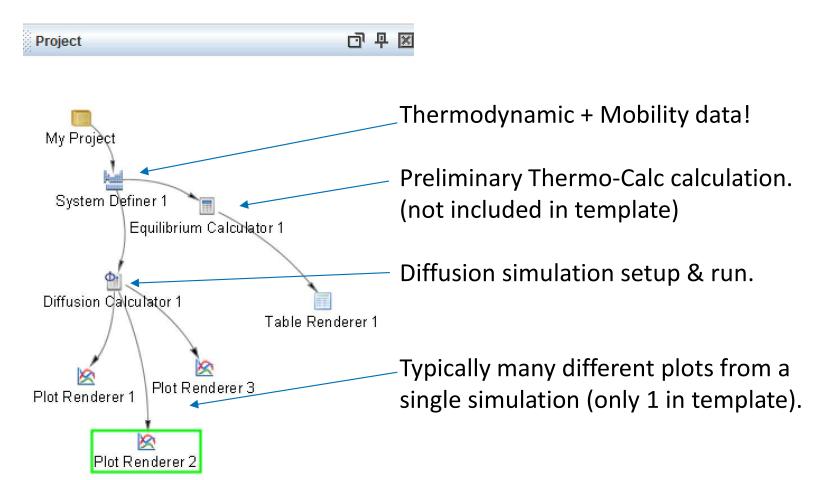




Conditions that apply to region boundaries (can be functions of time and temperature).

DICTRA Project in Graphical mode





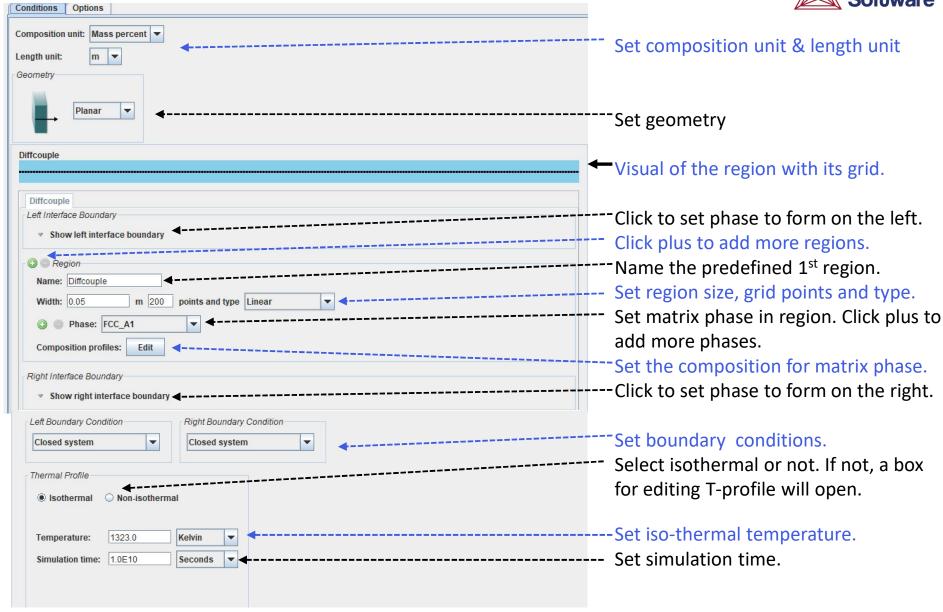
Typical calculation setup - Graphical



- 1. Select thermodynamic and kinetic data
- 2. Choose units for composition and distance
- 3. Enter geometry
- 4. Enter region(s)
- 5. Enter grid(s) in region(s)
- 6. Enter phase(s) in region(s)
- 7.Enter composition(s) for the phases
- (8. Set boundary conditions)
- 9. Set condition for temperature
- 10. Set simulation time
- 11. Perform simulation

Diffusion Calculator in Graphical mode

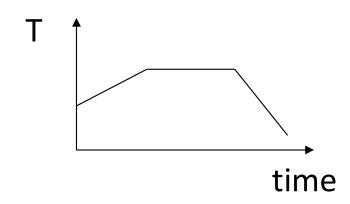




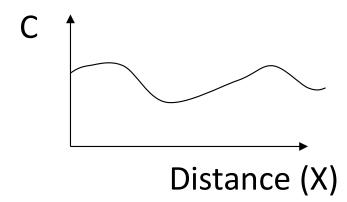
Input of T and c – Console mode



- ☐ Temperature (T) can be entered as a function of time (and distance)
- ☐ Many different functions can be used
 (+, -, *, **, SQRT(X),
 EXP(X),LOG(X),SIN(X))

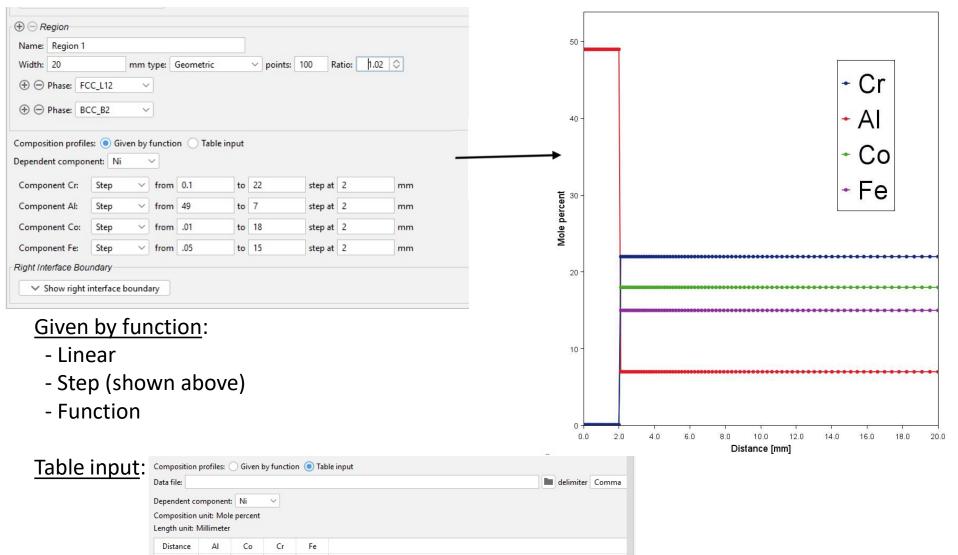


- Initial concentration can be entered as a function of distance or read from a file
- □ Special functions e.g. error-functions (erf(x)) and heaviside step functions (hs(x)) can be used.



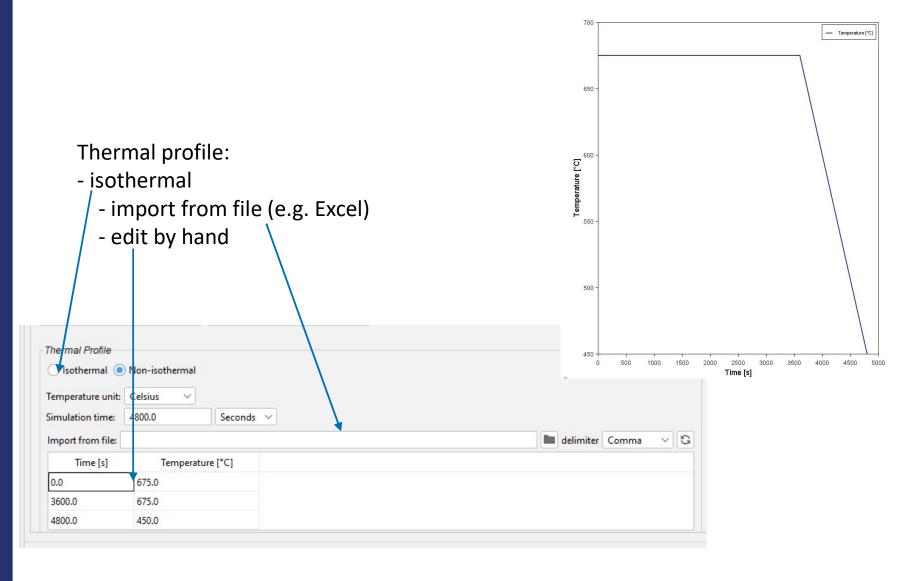
Input of composition – Graphical mode





Input of Thermal profile – Graphical mode







One phase Example

- Uphill diffusion

Uphill diffusion in a Fe-Si-C alloy



- In a classic experiment (published 1949), L.S. Darken welded together two steels having similar C-contents, but with different Si-contents.

Steel 1	Steel 2
3.8 %Si	0.05 %Si
0.49 %C	0.45 %C

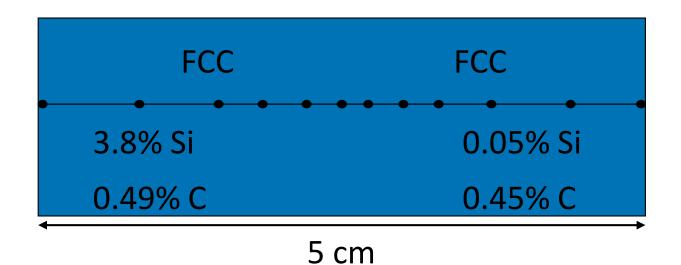
- After annealing Darken was able to conclude that C had diffused up its own concentration gradient, so-called "uphill diffusion". Darken thereby proved that it is the difference in C-activity rather than the difference in C-concentration that is the driving force for diffusion.

Darken, Trans AIME 180(1949)430

DICTRA Setup

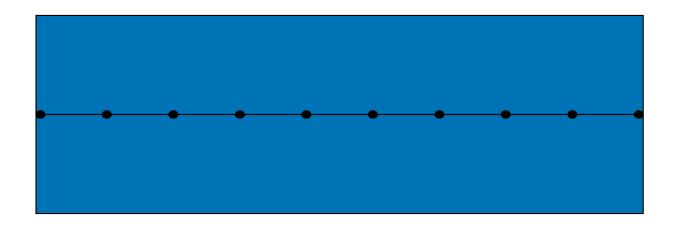


- One single region entered.
- Only FCC entered into this region, i.e. single-phase.
- Composition profiles entered with a step in center.
- Closer spacing between grid points towards the center.
- Global conditions: Constant temperature, T=1050 C.
- Boundary conditions: Zero-flux (= closed system).



Linear grid

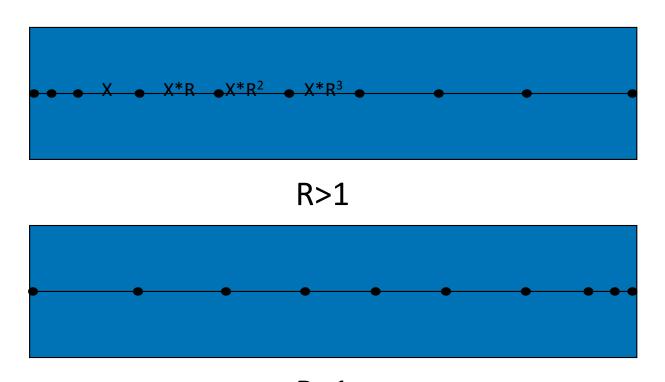




Equidistant distribution of node points.

Geometric Grid

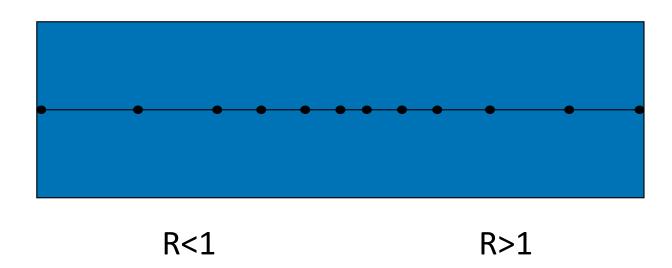




R<1 Node points represents geometric series

Double Geometric Grid





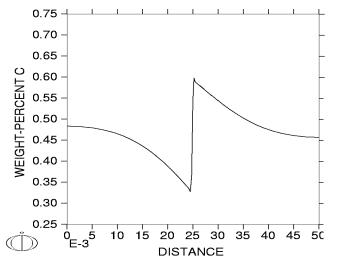
Uphill diffusion



Activity-profile for C

$$J_k = -\sum_{j=1}^{n-1} D_{kj}^n \frac{\partial c_j}{\partial z} \quad \Rightarrow \quad J_C = -D_{CC}^{Fe} \frac{\partial c_C}{\partial z} - D_{CSi}^{Fe} \frac{\partial c_{Si}}{\partial z}$$

Concentration-profile for C



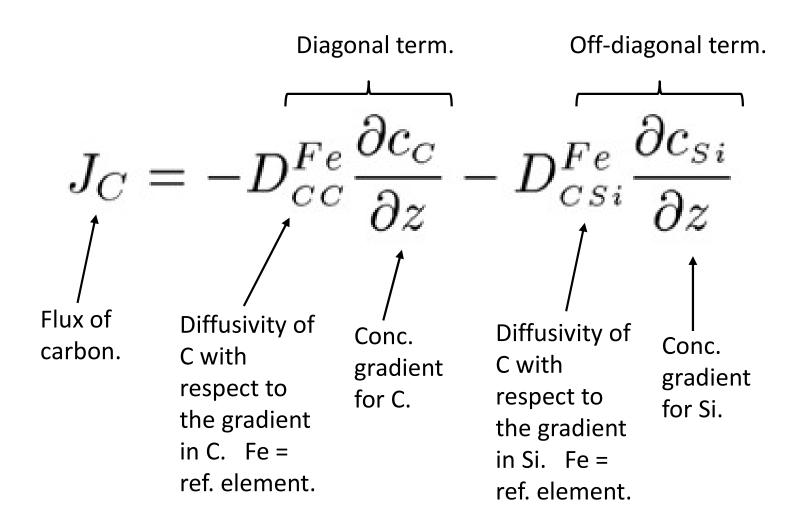
"Off-diagonal" term

Can cause uphill diffusion

51 48 Concentration-profile for Si 45 42 AC(C) 3.5 36 3.0 WEIGHT-PERCENT SI 33 2.5 30 27 -E-3 2.0 40 45 50 10 15 20 25 30 35 DISTANCE 1.0 0.5 20 25 30 35 40 45 50 Darken, Trans AIME 180(1949)430 10 15 DISTANCE

Uphill diffusion







Q & A

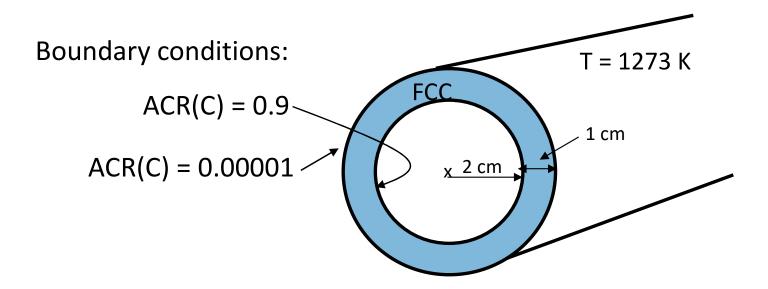


One phase Example

- Carburisation

Example – diffusion through a tube wall





<u>Demonstrates the use of:</u>

- Geometries
- Boundary conditions
- Reference states

Steel composition:

Fe - 0.6Mn - 0.7Si - 0.05C (wt-%)

DICTRA Geometries





Infinitely wide plate of a certain thickness.



Infinitely long cylinder of a certain radius.



Sphere with a certain radius.

Boundary conditions



In Graphical Mode:

Closed System (this is default)
Mixed zero flux and activity (Very useful!)
Composition

There are more possible boundary conditions in Console Mode:

Fix flux value (very theorethical)

Potential/Activity flux function (for real specialists)

Iterative activity flux function (for real specialists)

Gas (allows for growing/shrinking region)

Reference state

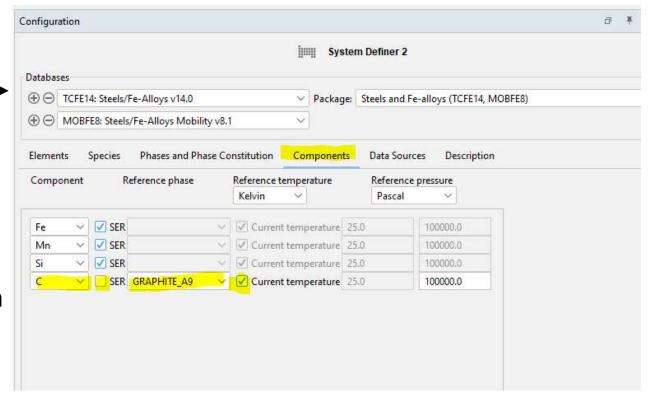


Database reference state: SER (Stable Element Reference).

SER - the element is referred to H of its stable phase at T=298.15 K, 1 atm plus its S at OK (= 0). This is practical for a database but **NOT** for comparison with measured activities and enthalpies.

The reference state can be changed in the software.

A changed ref. state can be indicated with addition of the letter R. AC(C) - activity of C ACR(C) - activity of C with a changed ref. state.



U-fraction



The composition variable used internally in DICTRA

"Mole fraction with respect to substitutional elements only"

Natural choice if it is assumed that

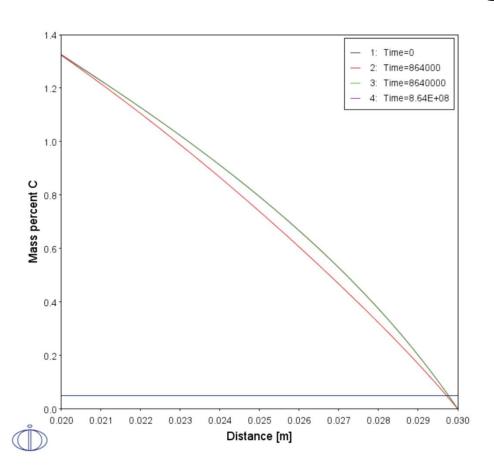
- •The partial molar volume is the same for all substitutional elements (V_s)
- •The partial molar volume is zero for all interstitial elements

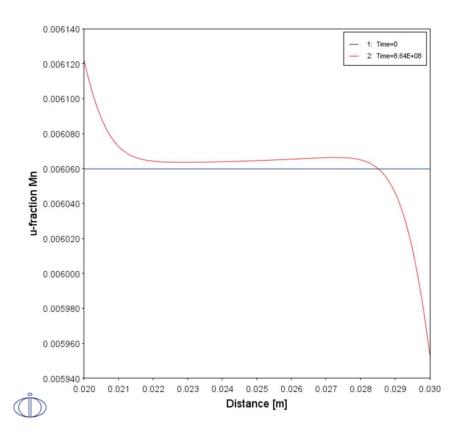
Example: System Fe-Cr-C, u_k is u-fraction, x_k is mole fraction

$$u_{Cr} = \frac{x_{Cr}}{x_{Cr} + x_{Fe}} = \frac{x_{Cr}}{1 - x_{C}}$$
 $u_{Fe} = \frac{x_{Fe}}{x_{Cr} + x_{Fe}}$ $u_{C} = \frac{x_{C}}{x_{Cr} + x_{Fe}}$ $u_{Cr} + u_{Fe} = 1$ $c_k = u_k/V_S$ [mol/m³]

Results - diffusion through a tube wall









Moving Phase boundary Example

- Growth of a particle

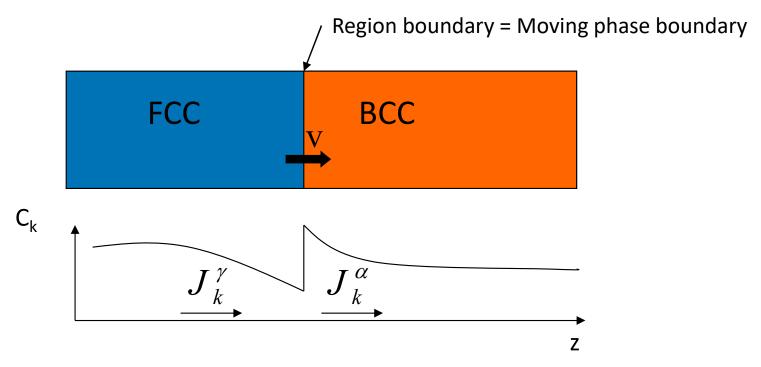
Moving Phase Boundary Calculations



- ☐ Used for calculating growth or dissolution of a phase
- ☐ Assumptions:
 - ✓ Local equilibrium holds at the phase boundary, i.e. concentrations at the boundary can be calculated from an equilibrium calculation in Thermo-Calc.
 - ✓ Diffusion controls the movement of the phase boundary
- ☐ Application examples:
 - Carbide dissolution
 - Solidification
 - \bullet Growth of σ -phase in a stainless steel

Moving phase boundary simulation





Solve diffusion equation in each phase

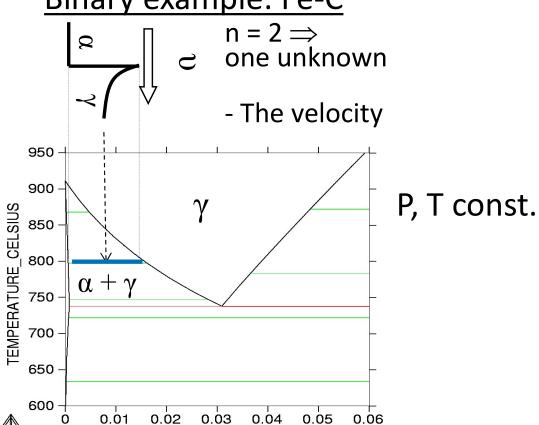
Calculate displacement of phase boundary

Thermo-Calc is used to find tie-lines

Diffusion with a moving interface





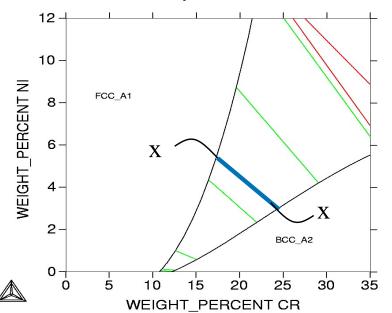


MOLE_FRACTION C

Ternary example: Fe-Cr-Ni

 $n = 3 \Rightarrow two unknowns!$

- One a_i or μ_i (i.e. one tie-line)
- The velocity



Moving Phase Boundary



- Moving phase boundary simulations may be set up in DICTRA in two different ways:
 - 1) Introducing two or more adjacent regions containing different phases

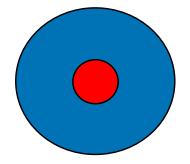
Phase 1 Phase 2

2) Entering an inactive phase (formed when thermodynamically stable)

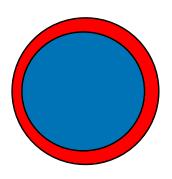
inactive phase 1

Some possible geometries

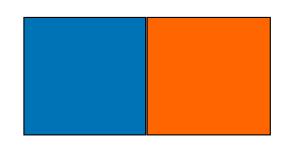




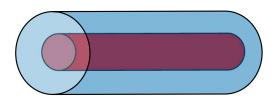
Growth or dissolution of a spherical precipitate



Growth of spherical film (Grain-boundary film)



Planar growth

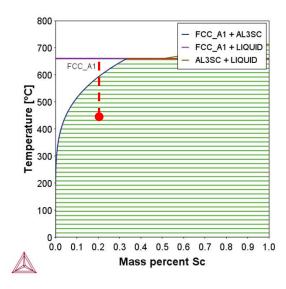


Growth of cylindrical precipitate

Example: Particle growth

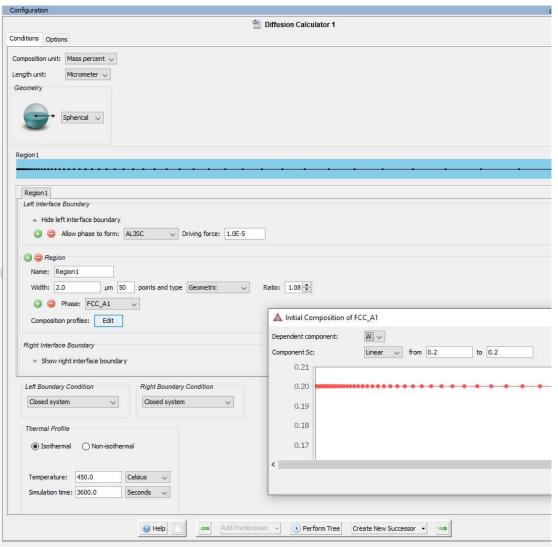


AI - 0.2 wt-% Sc



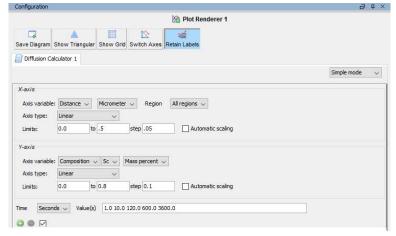
Quench to 450°C.

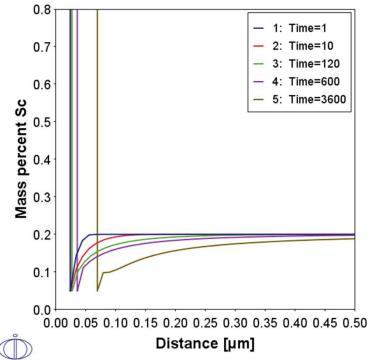
- → Supersaturated FCC
- → Driving force for the precipitation of Al₃Sc
- → Diffusion controlled growth of Al₃Sc

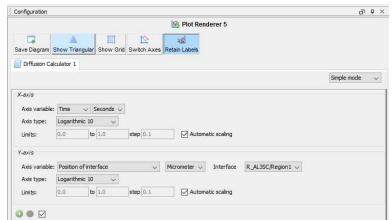


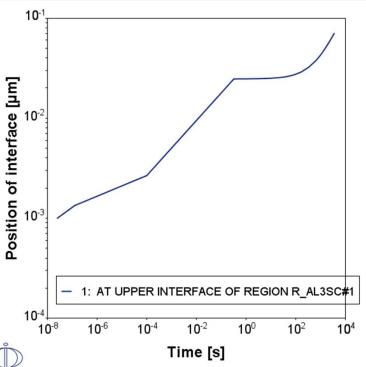
Results: Particle growth













Q & A

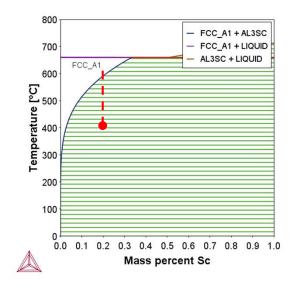


Home assignment 1

Home assignment 1: Particle growth



AI - 0.2 wt-% Sc



Try to make the Al-Sc simulation we just performed more realistic by adding the cooling from single-phase FCC at 600 °C to 450 °C.

Let's assume this cooling takes 2 seconds.

Does this change how much the phase interface has moved (i.e. how much the particle has grown) after 1 hour?

- 1) You have to change the setting to non-isothermal.
- Also consider how you can compare the two results after time=3600 s.